

I. Proving Trigonometric identities

1. Prove that $\sin^2 A - \cos^2 A = 2\sin^2 A - 1 = 1 - 2\cos^2 A$.
2. Prove that $\sin x(\operatorname{cosec} x - \sin x) = \cos^2 x$.
3. Prove that $(\sin A + \cos A)^2 + (\sin A - \cos A)^2 = 2$.
4. Prove that $(1 + \tan A)^2 + (1 - \tan A)^2 = 2\sec^2 A$.
5. Prove that $(\cot A - 1)^2 + (\cot A + 1)^2 = 2\operatorname{cosec}^2 A$.
6. Prove that $\frac{\operatorname{cosec} A}{\operatorname{cosec} A - 1} + \frac{\operatorname{cosec} A}{\operatorname{cosec} A + 1} = 2\sec^2 A$.
7. Prove that $\frac{\sec A}{\sec A - 1} + \frac{\sec A}{\sec A + 1} = 2\operatorname{cosec}^2 A$.
8. Prove that $\frac{1 + \sin \theta}{\cos \theta} + \frac{\cos \theta}{1 + \sin \theta} = 2\sec \theta$.
9. Prove that $\frac{\sin A}{1 + \cos A} + \frac{1 + \cos A}{\sin A} = 2\operatorname{cosec} A$.
10. Prove that $\frac{1 + \sin A}{\cos A} = \frac{\cos A}{1 - \sin A}$.
11. Prove that $\tan x + \cot x = \sec x \cdot \operatorname{cosec} x$.
12. Prove that $\sec^2 x + \operatorname{cosec}^2 x = \sec^2 x \cdot \operatorname{cosec}^2 x$.

II. Finding values of other T-function(Given one function)

1. If $\sin \theta = \frac{3}{5}$, find $\cos \theta$ and $\tan \theta$ (θ is acute).
2. If $\cos \theta = \frac{\sqrt{3}}{2}$, find $\sin \theta$ and $\tan \theta$ (θ is acute).
3. If $\sin \theta = \frac{5}{13}$, find $\sec \theta$ (θ is acute)
4. If $\cos \theta = \frac{4}{5}$ and θ is in the first quadrant, find $\sin \theta$ and $\tan \theta$.
5. If $\tan \theta = \frac{3}{4}$ and θ is in the third quadrant, find $\sec \theta$ and $\sin \theta$.
6. If $\sin A = \frac{1}{2}$ and B is in the first quadrant, find other t-functions.
7. If $\cos \theta = \frac{-4}{5}$ and θ is in the third quadrant, find the remaining t-functions of θ .
8. If $\cos x = \frac{-4}{5}$ and x is in the second quadrant, find the remaining t-functions of x .
9. If $\cot A = \frac{-15}{8}$ and A lies in the fourth quadrant, find the remaining t-functions.

10. If $\sin B = \frac{3}{5}$ and B is in the second quadrant, find other t-functions.

11. If $\sin \theta = \frac{-3}{5}$, θ is in the third quadrant, find the value of $\frac{4 \sec \theta + 3 \cot \theta}{4 \tan \theta + 5 \cos \theta}$.

III. Values of T- functions at standard angles

1. Show that $\sin 60^\circ \cdot \cos 30^\circ - \cos 60^\circ \cdot \sin 30^\circ = \frac{1}{2}$.

2. Find the value of $\cos 30^\circ \cdot \cos 60^\circ + \sin 30^\circ \cdot \sin 60^\circ$.

3. Find the value of $\cos 45^\circ \cdot \cos 60^\circ - \sin 45^\circ \cdot \sin 60^\circ$.

4. Find the value of $\sin 30^\circ \cdot \cos 60^\circ + \cos 30^\circ \cdot \sin 60^\circ$.

5. Prove that $\tan^2 30 + \tan^2 45 + \tan^2 60 = \frac{13}{3}$.

6. Evaluate $\tan^2 60^\circ + 3 \tan^2 45^\circ$.

7. Verify that $\sin 2\theta = \frac{2 \tan \theta}{1 + \tan^2 \theta}$ if $\theta = 30^\circ$.

8. Verify that $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$ if $\theta = 30^\circ$.

9. Evaluate $4 \sin^3 \frac{\pi}{3} - 3 \cos \frac{\pi}{6}$.

10. Evaluate $\frac{\sin^2 \frac{\pi}{3} + \cos^2 \frac{\pi}{6}}{2 \sin \frac{\pi}{6} + 3 \tan \frac{\pi}{4}}$.

11. Prove that $\frac{\tan 60 - \tan 45}{1 + \tan 60 \cdot \tan 45} = 2 - \sqrt{3}$.

IV. Signs of T-functions in different quadrants

1. Determine the sign of the following:

(i) $\cos 140^\circ$ (ii) $\sin 340^\circ$ (iii) $\operatorname{cosec}(-20^\circ)$ (iv) $\tan 500^\circ$ (v) $\cos(-420^\circ)$

2. Determine the sign of the following, if $0 < \theta < 90$,

(i) $\sin(180^\circ - \theta)$ (ii) $\tan(270^\circ + \theta)$ (iii) $\operatorname{cosec}(90^\circ + \theta)$ (iv) $\sec(810^\circ + \theta)$ (v) $\cos(\theta - 540^\circ)$

3. Write down the signs of the following

(i) $\cot(1080^\circ + x)$, $0 < x < 90^\circ$ (ii) $\cot(-97^\circ)$ (iii) $\sec(360^\circ - x)$, $0 < x < 90^\circ$

V. Graph of T-functions

1. Draw the graph of $y = \sin 2x$. 2. Draw the graph of $y = \sin 3x$. 3. Draw the graph of $y = \cos 2x$.